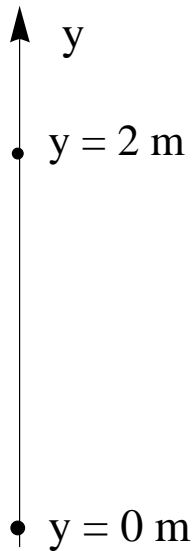


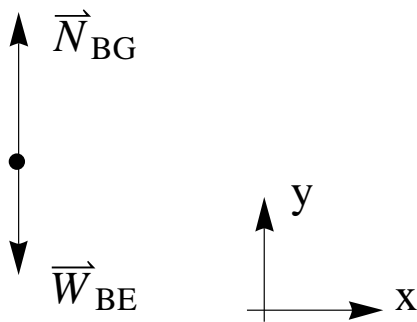
Example 1:



The ball is dropped from rest ($v_1 = 0$) at a height of $y_1 = 2 \text{ m}$. Its velocity just before hitting the ground \vec{v}_2 is given by

$$v_2^2 - 0^2 = -2g(0 - 2) \implies \vec{v}_2 = -\sqrt{2 \times 9.8 \times 2} \vec{j} = -6.3 \vec{j} \text{ m/s}.$$

While the ball is colliding with the ground, two forces are acting on the ball, the weight \vec{W}_{BE} and the normal by the ground \vec{N}_{BG} .



\vec{F}_{net} is always along the y-direction and is $(N_{\text{BG}} - m g) \vec{j}$. If we apply the impulse momentum theorem between

$t_i = 10 \text{ ms} =$ instant just before the collision with the ground when

$$\vec{v} = \vec{v}_i = -6.3 \vec{j}$$

and

$t_f = 20 \text{ ms} =$ instant just after the collision with the ground when $\vec{v} = \vec{v}_f$

we get

$$m(\vec{v}_f - \vec{v}_i) = \int_{t_i}^{t_f} \vec{F}_{\text{net}} dt$$

or since all of the vectors have only y-components

$$m(v_f - v_i) = \int_{t_i}^{t_f} F_{\text{net}} dt = \int_{t_i}^{t_f} N_{\text{BG}} - m g dt = \int_{t_i}^{t_f} N_{\text{BG}} dt - m g (t_f - t_i)$$

The integral $\int_{t_i}^{t_f} N_{\text{BG}} dt$ is the area under the $N_{\text{BG}}(t)$ curve and is equal to

$$\frac{480 (20-10) 10^{-3}}{2} = 2.4 \text{ N.s}$$

Also

$$m g (t_f - t_i) = 0.2 \times 9.8 (20 - 10) 10^{-3} = 0.02 \text{ N.s}$$

Notice that most of the impulse is due to the normal force.

The velocity just after the ball bounces off the ground is then

$$v_f = v_i + \frac{\int_{t_i}^{t_f} N_{\text{BG}} dt - m g (t_f - t_i)}{m} = -6.3 + \frac{2.4 - 0.02}{0.2} = 5.6 \text{ m/s}$$

The ball reaches a height h such that

$$0^2 - v_f^2 = -2 g h \implies h = 1.6 \text{ m}$$